

# Chapter 11

## FSM Reverse Engineering

### SKEE2263 Digital Systems

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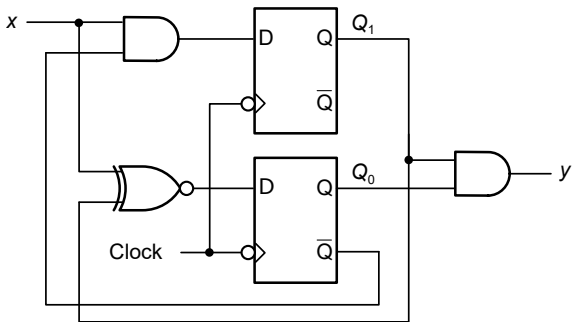
# Reverse Analysis / Analysis

## What is Reverse Engineering?

Work in reverse direction to derive the state diagram from a given circuit.

- Determine circuit model - Moore or Mealy
- Find:
  - 1 Number of states
  - 2 Next state and output equations
  - 3 Next state and and output K-maps
- Get State table
- Draw the state diagram

## Determine Machine Type



### ■ Moore or Mealy?

- ⇒ AND inputs connects only to FF outputs
- ⇒ output depends only on present state
- ∴ this is a Moore machine

## Circuit $\rightarrow$ Equations

**1** #FF: 2

$\Rightarrow$  Number of states = 4

**2** Next state equations

$$Q_1^+ = D_1 = Q_0'x$$

$$Q_0^+ = D_0 = \overline{Q_1 \oplus x} = Q_1x + Q_1'x'$$

**3** Output equation

$$y = Q_1Q_0$$

# Equations $\rightarrow$ K-maps $\rightarrow$ minterms

		$x$	
		0	1
$Q_1Q_0$	00		1
	01		
	11		
	10		1

$$Q_1^+ = Q_0'x$$

$$= \Sigma(1, 5)$$

		$x$	
		0	1
$Q_1Q_0$	00	1	
	01	1	
	11		1
	10		1

$$Q_0^+ = Q_1x + Q_1'x'$$

$$= \Sigma(0, 2, 5, 7)$$

		$Q_0$	
		0	1
$Q_1$	0		
	1		1

$$y = Q_1Q_0$$

## Alternative: Equations $\rightarrow$ Canonical SOP minterms

$$\begin{aligned}Q_1^+ &= Q_0'x \\ &= Q_0'x(Q_1 + Q_1') \\ &= Q_1'Q_0'x + Q_1Q_0'x \\ &= \Sigma(1, 5)\end{aligned}$$

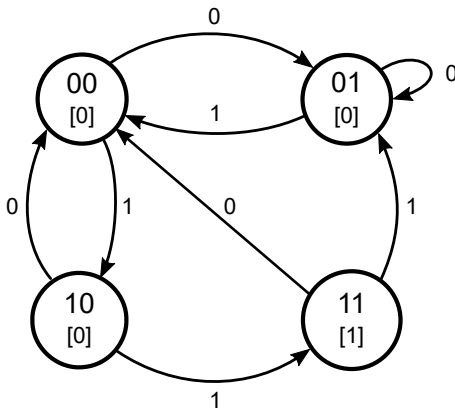
$$\begin{aligned}Q_0^+ &= \overline{Q_1 \oplus x} = Q_1x + Q_1'x' \\ &= Q_1x(Q_0' + Q_0) + Q_1'x'(Q_0' + Q_0) \\ &= Q_1Q_0'x + Q_1Q_0x + Q_1'Q_0'x' + Q_1'Q_0x' \\ &= \Sigma(0, 2, 5, 7)\end{aligned}$$

## Minterms $\rightarrow$ State Table

Present State	Input	Next State	Output
$Q_1Q_0$	$x$	$Q_1^+Q_0^+$	$y$
00	0	01	0
	1	10	
01	0	01	0
	1	00	
10	0	00	0
	1	11	
11	0	00	1
	1	01	



# State Table $\rightarrow$ State Diagram





## Circuit $\rightarrow$ Equations

**1** #FF: 2

$\Rightarrow$  Number of states = 4

**2** Next state equations

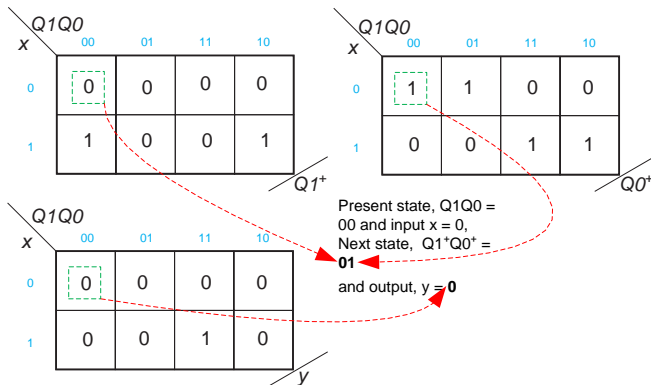
$$Q_1^+ = D_1 = Q_0'x$$

$$Q_0^+ = D_0 = \overline{Q_1 \oplus x} = Q_1x + Q_1'x'$$

**3** Output equation

$$y = Q_1Q_0x$$

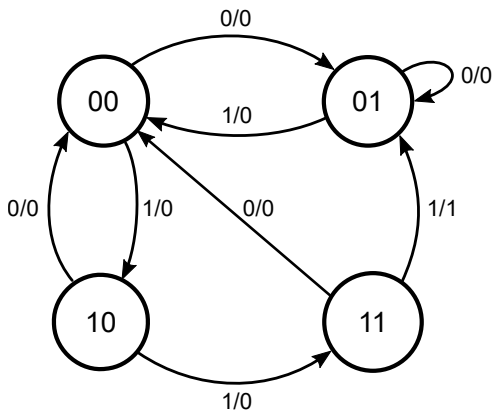
# Equations $\rightarrow$ K-maps



## Trick

Derive state diagram directly from K-maps

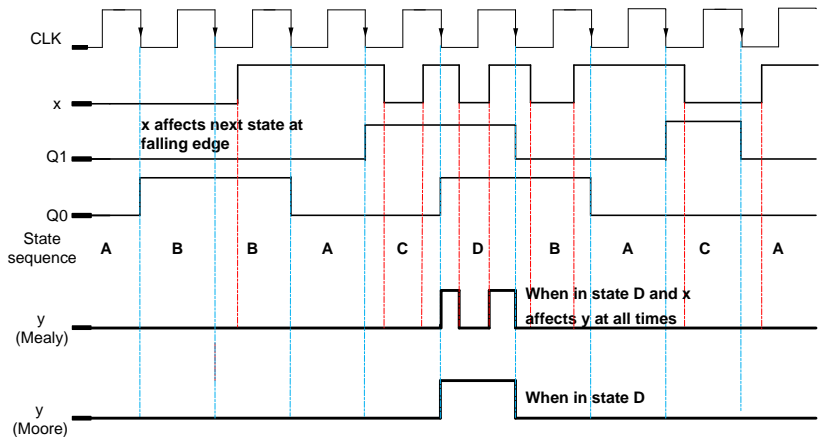
## K-maps $\rightarrow$ State Diagram



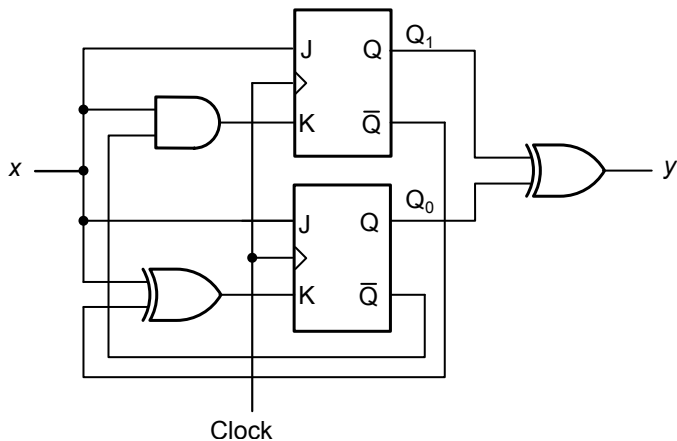
## State Table for Reference

Present State	Input	Next State	Output
$Q_1Q_0$	$x$	$Q_1^+Q_0^+$	$y$
00	0	01	0
	1	10	0
01	0	01	0
	1	00	0
10	0	00	0
	1	11	0
11	0	00	0
	1	01	1

# Waveforms of Both Moore & Mealy Machines



## Determine Machine Type



- This is a Moore machine



## Circuit $\rightarrow$ FF Input Equations

Flip-Flop input equations:

$$\begin{array}{ll} J_1 = x & J_0 = x \\ K_1 = Q_0'x & K_0 = Q_1 \oplus x \end{array}$$

Output equation:

$$y = Q_1 \oplus Q_0$$

## FF Input Eqs $\rightarrow$ Next State Eqs (EXTRA STEP)

JKFF characteristic equations:

$$JQ' + K'Q$$

Substituting:

$$\begin{aligned} Q_1^+ &= J_1Q_1' + K_1'Q_1 \\ &= xQ_1' + [Q_0'x]'Q_1 \\ &= Q_1'x + [Q_0'' + x']Q_1 \\ &= Q_1'x + Q_1Q_0 + Q_1x' \\ &= \Sigma m(1, 3, 4, 6, 7) \end{aligned}$$

$$\begin{aligned} Q_0^+ &= J_0Q_0' + K_0'Q_0 \\ &= xQ_0' + [Q_1' \oplus x]'Q_0 \\ &= Q_0'x + Q_0[Q_1'x + Q_1x'] \\ &= Q_0'x + Q_1'Q_0x + Q_1Q_0x' \\ &= \Sigma m(1, 3, 5, 6) \end{aligned}$$

## Minterms $\rightarrow$ State Table

Present State	Input	Next State	Output
$Q_1Q_0$	$x$	$Q_1^+Q_0^+$	$y$
00	0	00	0
	1	11	
01	0	00	1
	1	11	
10	0	10	1
	1	01	
11	0	11	0
	1	10	

## State Table → State Diagram

